

# PARAMETRIC STUDY FOR INFLUENCE OF INPUT PARAMETERS FOR ANALYSIS OF FIBRE REINFORCED CONCRETE SLAB-SOIL INTERACTION

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**Abstract.** For geotechnical engineering and design of foundation elements of structures is important to properly determine the stress-deformation state of the subsoil. The calculation is most often done using the finite element method and the computational models. This article includes the parametric study for the selected type of concrete foundation structures. The article focuses attention to the calculation of the deformation of the slab with respect to the influences of individual input parameters (e.g. stiffness of concrete and subsoil, boundary condition, size of elements). Calculations are performed for two concrete types and three soil variants.

## Keywords

*Geotechnical engineering, foundation elements, structures, subsoil, finite element method, 3D computational model, concrete, calculation.*

## 1. Introduction

Analysis of the concrete structure in interaction with the subsoil is a complex computational task and research area [1], [2]. This area has a great deal of attention in the research in the world [3], [4], [5]. For this task is also typical influence of physical and structural nonlinearity. This is particularly the case when the construction collapse and total bearing capacity are monitored. With these reasons, it is important experiments research [6], [7], [8]. Subsequently, it is possible to use appropriate numerical and design methods. Design models of punching of flat

slabs and geotechnical tasks are being surveyed and discussed [9], [10], [11]. To achieve comprehensible numerical results, the core of problem is to be understood. It is advisable to initially solve the problem as linear and to know the basic behavior of the structure. In the numerical task being solved, the ratio is the stiffness of the concrete structure and the subsoil and the model uncertainty. Numerical calculations of deformations for the concrete slab in interaction with the subsoil are also influenced by the choice of ground and soil model. There are a number of design and numerical methods to solve the task of interacting slab with the subsoil. Typical cases include the use of analytical methods that often simplify the solution. The limitation is that it is not possible to change the properties of the subsoil model in parts or it is not possible to examine closely the collapse of the structure. On the other hand, it is possible to use the finite element method [12], [13]. The Finite Element Method was used in this paper through the ANSYS computational program [14]. In this method and task, however, a whole range of options and parameterization of the computational model was created. With this advanced calculation method, it is possible to take into account the actual behavior of the problem solved. The computational model is based on discretization of finite elements and material models. Some approaches use advanced methods and calculations are in [15], [16], [17]. This article aims at this research area.

## 2. Experimental testing

An integral part of the study of interaction between the concrete slab and the subsoil is experimental testing. VSB

- Technical University, Faculty of Civil Engineering [18] has for this purpose specialized equipment/device. This equipment has of a test frame with a hydraulic press with a capacity of 1000 kN. This test equipment/device is connected to a universal measurement panel for deformation, strain and force. Concrete slabs can have a size up to 2000x2000 mm and a typical thickness of 100 to 200 mm. Typical tested concrete slab during and after the test is shown in the Figures 1 and 2. The subsoil has typical  $E_{def}$  values of 3 to 33 MPa.



Fig. 1: Concrete slab-production



Fig. 2: Concrete slab - after the test

With the development of material research, there are a number of designs used. Selected experiments and calculations for solved slabs are in [19] and [20]. Typically, fibre concrete is show for example. This material has a number of improved properties. For example: tensile strength and ductility. For the already implemented experimental program, computational models and analyses are created that appropriately respect the actual behaviour. Concrete slabs also contain from 0 to 75 kg/m<sup>3</sup> of fibre [21]. For this series of fibre concrete slabs, the total bearing capacity of the slabs was in the range of 300 to 700 kN. Details of the experimental program with fibre concrete slabs are given [21]. The fibre concrete slab G02 is selected for a parametric study. This concrete slab had a maximum total bearing capacity of up to about 500 kN. The loading record of during the test is shown in Figure 3. Further data of experiments on specialized

equipment/device and calculations has [22]. Typical used fiber for concrete slab are shown in Figure 4.

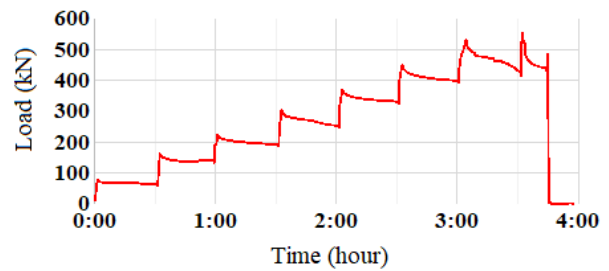


Fig. 3: Loading record of during the test [21]

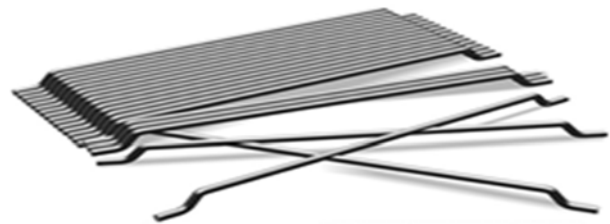


Fig. 4: Fiber Dramix 3D 65/60 BG [21], [23]

### 3. Parametric study

The subject of the parametric study is to evaluate the influence of the input variables on the calculation. The study solves the size of the deformation for different combinations of the modulus of elasticity of the concrete and the subsoil, the size of the finite element and the depth of the subsoil. The modelling task represents a typical case of experiment of concrete slab for specialized equipment. Parametric study for the subsoil model considers depths of 4, 6 and 8 m. The calculation was done in ANSYS [14]. The solved task offers several possibilities of creating a computational model. The task is also symmetrical for both axes. It is simplest to use only the beam model on the subsoil. A more advanced choice is a planar and spatial computational model. With regard to the parameters calculation and the computational complexity is selected for computational model used finite element PLANE 182 (Figure 5). The computational model consists of the final elements of PLANE 182 which will adequately capture the solved area of the parametric study. PLANE182 [14] is used to model 2-D solid structures. It can be used as either a plane element (plane stress, plane strain or generalized plane strain) or an axisymmetric element with or without torsion. In most cases, the element is defined by four nodes with two degrees of freedom at each node: translations in the nodal  $x$  and  $y$  directions [14].

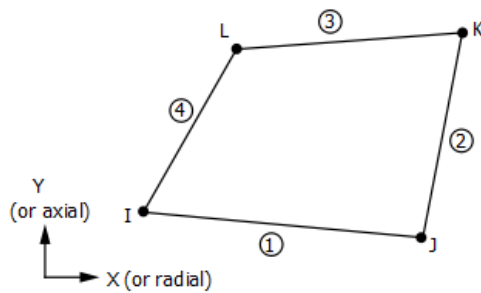


Fig. 5: PLANE182 Geometry [14]

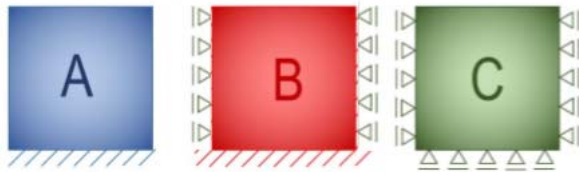


Fig. 6: Boundary conditions

The basic size of the finite element is set to the line size of 0,1 m. Additionally a comparison of the influence of the size of the finite element is performed for the selected case of the calculation model. For the basic part of the study a computational model with parameters is chosen: the modulus of elasticity of the concrete is 28 GPa and the base has a stiffness of 5 to 35 MPa.

### 3.1. Influence of boundary conditions

The first comparison presents the effect of boundary conditions. The variance of the boundary conditions is shown in Fig. 6. The calculation is performed for the modulus of elasticity for concrete 28 GPa and subsoil of 15 MPa. The depth of the subsoil is 8 m. The results are shown in Table 1.

Tab.1: Vertical deformation - Boundary conditions

28 GPa / 15 MPa	Deformation [mm]		
	Boundary conditions		
Depth [m]	A	B	C
Top surface of concrete	26.16	24.98	24.99
Top surface of subsoil (0)	26.15	24.97	24.98
2	15.45	14.44	14.42
4	8.62	8.06	8.09
6	3.75	3.66	3.71
8	0.00	0.00	0.00

### 3.2. Influence of element size

A comparison of the influence of the size of finite element was also performed. The calculation has three variants. The finite elements have an edge size of 0.025; 0.1; 0.25 m. The results are shown in Tab. 2. Percentage is given as compared to the base size of the finite element of 0.1 m.

Tab.2: Vertical deformation – Size of finite element

Mesh	Deformation [mm]		
	Finite element [m]		
Depth [m]	0.250	0.100	0.025
Top surface of concrete	25.573	26.160	26.448
%	97.756 %	-	101.101 %
Top surface of subsoil (0)	25.572	26.151	26.432
%	97.786 %	-	101.075 %

### 3.3. Influence of concrete stiffness

Another part of the study solves the stiffness of concrete material for 8 m deep subsoil. Two variants of 28 and 50 GPa are considered. It is for calculation: concrete modulus of elasticity of 50 GPa, 35 MPa and subsoil track bed depth of 8 m. The fig. 7 show details on deformation information. This is a calculation: modulus of elasticity of concrete 50 GPa and subsoil 35 MPa and depth 8 m.

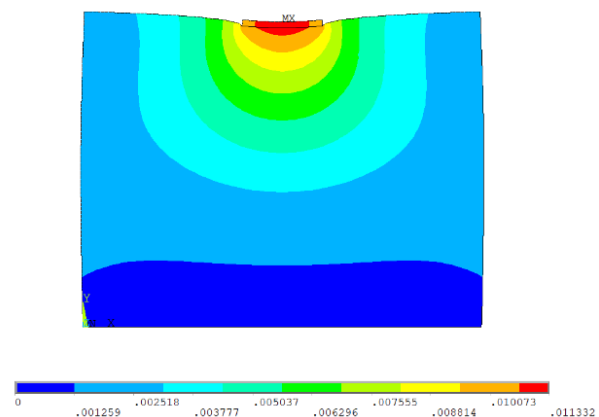


Fig. 7: Vertical deformation (11.332 mm) for concrete (50 GPa) and subsoil (35 MPa)

A summary comparison is shown in Table 3. Differences in deformations are small.

Tab.3: Vertical deformation – Modulus of elasticity concrete 28 and 50 GPa

50 GPa	Deformation [mm]		
	Subsoil		
Depth [m]	35 MPa	15 MPa	5 MPa
Conc.*	11.33	25.72	75.91
0	11.33	25.71	75.90
2	6.62	15.44	46.28
4	3.69	8.63	25.89
6	1.61	3.76	11.27
8	0.00	0.00	0.00

\* Top surface of concrete

28 GPa	Deformation [mm]		
	Subsoil		
Depth [m]	35 MPa	15 MPa	5 MPa
Conc.*	11.68	26.16	76.41
0	11.68	26.15	76.40
2	6.63	15.45	46.29
4	3.69	8.62	25.89
6	1.61	3.75	11.27
8	0.00	0.00	0.00

### 3.4. Influence of elasticity of subsoil

The last part of the parametric study deals with the comparison of the modulus of elasticity and the depth of the subsoil. The modulus of elasticity of the concrete is 28 GPa. The modulus of elasticity of the subsoil has values of 5.15 and 35 MPa. The depth of the subsoil is 4, 6 and 8 m. The following graph in Figure 8 shows the dependence of depth of the subsoil model on the resulting deformations for the elastic modulus of 35 MPa.

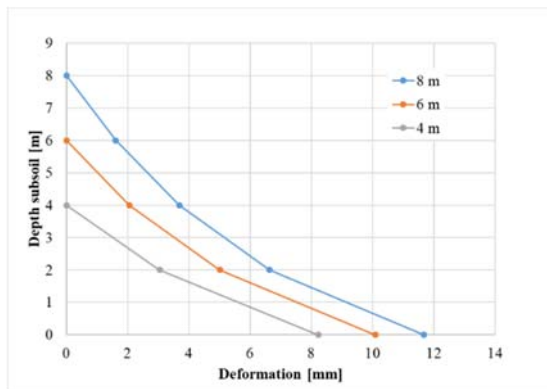


Fig. 8: Vertical deformation (11.332 mm) for concrete (50 GPa) and subsoil (35 MPa)

The results can also be summarized in Figure 9.

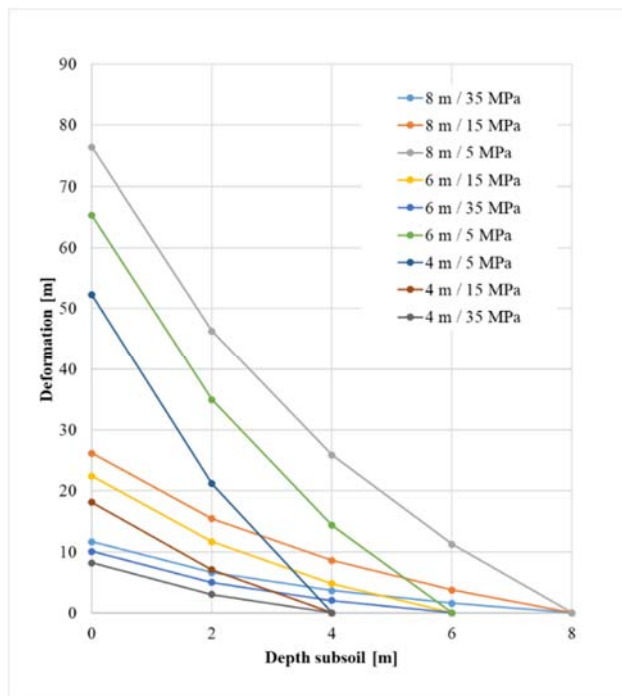


Fig. 9: Vertical deformation (mm) for concrete (28 GPa) and subsoil (5, 15 a 35 MPa) and depth (4; 6; 8 m)

When choosing depths of the subsoil, it is also possible to consider the magnitude/size of the stress. This problem compares tab. 4. Calculations of the deformation as well

as the normal stress  $\sigma_y$  are shown in the calculations. The calculation is made for the modulus of elasticity of concrete 28 GPa and the modulus of elasticity of subsoil 15 MPa.

Tab.4: Vertical deformation and stress  $\sigma_y$

28 GPa/ 15 MPa	Calculation model - Depth 6-8 m				Difference percentage	
	Def.	Stress $\sigma_y$	Def.	Stress $\sigma_y$	Def.	Stress $\sigma_y$
Depth [m]	mm	kPa	mm	kPa	%	%
Top surface of concrete	26.16	-4,203.00	22.45	-4,203.00	1.17	1.00
Top surface of subsoil (0)	26.15	-105.01	22.44	-105.20	1.17	1.00
2	15.45	-61.49	11.66	-62.08	1.32	0.99
4	8.62	-40.31	4.79	-41.23	1.80	0.98
6	3.75	-31.38	0.00	-32.23	-	0.97
8	0.00	-26.38	-	-	-	-

## 4. Discussion with results of experiment

The parametric study includes a variety of options to access the calculation of the slab and subsoil interaction. For comparing the calculated results, the information from the experiment in Fig. 10 is shown. The orientation of the slab is shown in Fig 11. The maximum measured deformation was 32.01 mm at point 6. The finite element method is based on the discretization of the computational model for the finite elements, nodes and integration points. The discretization of a model causes differences in results. The results for the different size of finite elements in the deformation are for the solved task of slab and subsoil few percent.

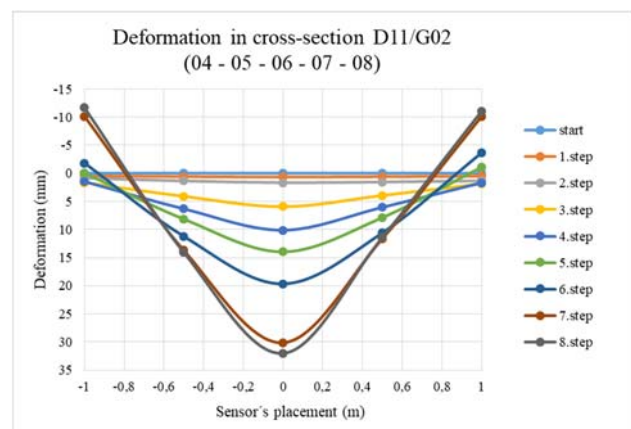


Fig. 10: Vertical deformation in cross-section D11/G02 (mm)



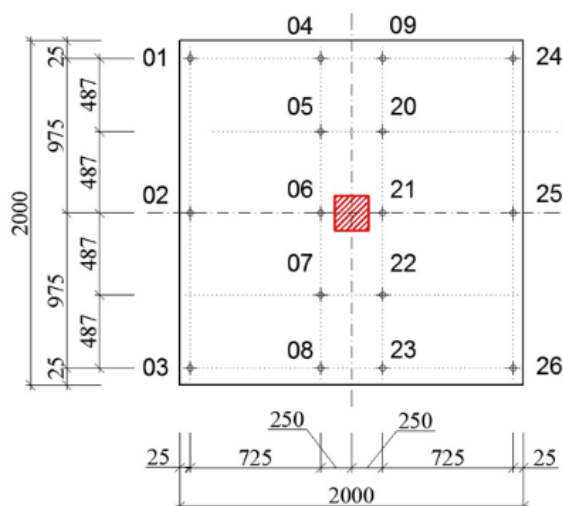


Fig. 11: Orientation of the concrete slab

The largest deformation for variant A was calculated in part of the parametric study containing different boundary conditions. Variant A included the supports only on the bottom of the computational model. Next calculations were performed for this boundary condition variant A. The influence of boundary conditions is considerably smaller than that of input parameters of concrete and subsoil. The ratio between the maximum deformation from the experiment and calculated, was around 78%. In comparison of the calculated deformations there are slight differences in comparison for different stiffness of the concrete. However, this is true for linear calculation. The size of the modulus of elasticity of the subsoil is of much greater importance.

For the calculation of deformation, the worst case is that the modulus of elasticity of the concrete is 28 GPa and the subsoil has a stiffness of only 5 MPa. The size of the deformation is 76.41 mm for this case. Maximal deformations it also depends on the vertical depth of the subsoil model. The largest deformation is for subsoil with a depth of 8 m. By comparing the results of the deformation of the slab and the calculations, it is possible to find the best match of numerical models with a modulus of elasticity of 15 MPa soil. The difference of deformations between the elastic modulus of the concrete 28 and 50 GPa is significantly smaller. In absolute value it is less than 1 mm. The last part of the calculation and study show that the depth of the subsoil affects the calculated deformation significantly more than the stress.

## 5. Conclusions

Interaction between the concrete slab and the subsoil is a complicated task. The calculations and studies have shown that the influence of input parameters can be great. Appropriate use of the subsoil with the modulus elastic with 15 MPa was shown. The concrete difference with the

modulus of elasticity 50 or 28 GPa is already small. Particularly in the case of the depth of the subsoil model, the calculated deformations can be very different. For the solved task, it is possible to consider the typical basic recommendation modelling of base depth of subsoil as 2x base widths of fundament as appropriate. The problem of the computational model is further complicated for cases of more complex geological conditions. This is especially a small modulus of elasticity for the subsoil. The results lead in further next detailed study and research of the interaction of the concrete slab and subsoil. Linear calculation and computational model provide not sufficient accuracy, and it would be preferable to choose a nonlinear model and calculation. Another goal is nonlinear calculation. Further research and numerical modelling is also concentrated with respect to the approach of calculation and using of subsoil models in [24]. However, this also requires more detailed information about the experiments.

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